

## 11 Lab 11 – April 28, 2022

Instead of a tutorial students have to solve homework 4 and submit solutions in Moodle

### Homework 6

**Example 1.** Form a linear difference equation which has the following general solution

$$\{a_n\}_{n=0}^{\infty} = \{\alpha + \beta n + \gamma (-2)^n\}_{n=0}^{\infty}; \alpha, \beta, \gamma \in \mathbb{R}.$$

**Example 2.** Given a non-homogeneous linear difference equation of order 3 with  $b_n = (6 - 2n^2)$ . Moreover, the characteristic equation of the associated homogeneous linear difference equation has roots  $\lambda_{1,2} = 1$ , and  $\lambda_3 = -4$  (i.e. the root  $\lambda = 1$  has multiplicity 2). What is the estimate of one solution of the non-homogeneous equation  $\hat{a}_n$ ?

**Example 3.** Solve the following difference equation

$$a_{n+2} - 3a_{n+1} + 2a_n = 6 \cdot 2^n, \quad a_0 = 2, a_1 = 6.$$

**Example 4.** Solve the following difference equation

$$a_{n+2} = 5a_{n+1} + 6a_n + (4n - 5) \cdot 3^{n+1}, \quad a_0 = 6, a_1 = 9.$$