

### Test 3 (11th December 2023)

**Task 1:** At a Christmas market kiosk, tourists can buy unflavored, vanilla-flavored, or almond-flavored hot chocolate. We observe the following frequencies of hot chocolates purchased by children and adults:

|          | unflavoured | vanilla-flavoured | almond-flavoured |
|----------|-------------|-------------------|------------------|
| children | 15          | 30                | 15               |
| adults   | 15          | 10                | 15               |

Test on the statistical level

- $\alpha = 5\%$  whether the numbers of child customers and adult customers are approximately the same, (3 points)
- $\alpha = 1\%$  whether the type of the chosen flavour depends on the age class (children vs. adults). (3 points)

**Task 2:** Consider a game with 4 levels. The probability of winning a level is 0.6, and a loss occurs with the remaining probability. When you win the  $i$ -th level, you jump to the next level, i.e. to the  $(i + 1)$ -th level (except when you win the 4th level, in which case you stay at the 4th level). When you lose the  $i$ -th level, you drop down 1 level, i.e. to the  $(i - 1)$ -th level (except when you lose the first level, in which case you stay at the first level). Find the transition probability matrix and the stationary distribution. (4 points)